

Research on ride comfort of vibratory rollers: Part-1 Study on the effect of different cab isolation mounts

Yan Kang¹, Vanliem Nguyen², Xiaoyan Guo³, Yuehan Li⁴

School of Mechanical and Electrical Engineering, Hubei Polytechnic University, Huangshi, 435003, China
Hubei Key Laboratory of Intelligent Conveying Technology and Device, Hubei Polytechnic University,
Huangshi, 435003, China

²Corresponding author

E-mail: ¹2812409316@qq.com, ²xuanliem712@gmail.com, ³184044288@qq.com, ⁴1024536715@qq.com

Received 6 January 2021; received in revised form 21 January 2021; accepted 29 January 2021

DOI <https://doi.org/10.21595/jmai.2021.21860>



Copyright © 2021 Yan Kang, et al. This is an open access article distributed under the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

Abstract. In order to evaluate the ride quality of vibratory roller's cab used the different isolation mounts including the traditional rubbers, hydraulics, and hydro-pneumatics, a nonlinear dynamics model of the vibratory roller under interaction of the deformable terrain and drum has been established based on Matlab/Simulink software. The root-mean-square (RMS) of the accelerations of the vertical driver's seat and the cab's pitch angle have been used as objective studies. The influence of damping and stiffness coefficients of different isolation mounts on the cab's ride quality has been respectively simulated and analyzed under a hard ground at an excitation 28 Hz of the vibration drum. The research results indicate that the characteristics of non-linear damper and high-static stiffness of the hydro-pneumatic mounts can greatly reduce the vertical driver's seat vibration and cab shaking when compared to vibratory roller's cab using the traditional rubber mounts and hydraulic mounts under stiffness and damping coefficients of the vehicle and cab isolations. Particularly with the dynamics parameters of $K_c = [0.8 \text{ to } 1.2] \times K_{c0}$, $C_c = [0.8 \text{ to } 1.0] \times C_{c0}$, $K_{t,d} = [0.6 \text{ to } 1.0] \times K_{t0,d0}$, and $C_{t,d} = [1.0 \text{ to } 1.2] \times C_{t0,d0}$.

Keywords: vibratory rollers, ride comfort, rubber mount, hydraulic mount, hydro-pneumatic mount, off-road terrains.

1. Introduction

The soil compactor often works in factories and construction site, and its operation process includes a combined static and dynamic forces of all the vehicle and the drum to compress the asphalt, terrain, or other materials. The vibration excitations from the deformable terrain and the drum are thus transmitted the driver via the cab and the vehicle's isolation systems. Consequently, the isolation system of the cab is one of the most important indexes for the improvement of the vehicle's ride quality.

Basic studies of the interaction between the wheel and deformable terrain [1-4] and of interaction between the elastic/plastic ground and drum [5] showed that the response in the vibration process of the vehicle had been strongly affected by terrains. Almost the isolation mounts of the cab of vibratory rollers were equipped by the traditional rubber with its high-stiffness coefficient and low-damping coefficient of the rubber materials [5, 6]. Thus, the high-stiffness of the rubber helped suppress only noise and vibration in the high frequency region, on the contrary, the low-damping coefficient of the rubber could generate the vibration with its high-magnitudes to reduce the ride quality of the vehicle [6]. The effect of designed dynamic parameters of the rubber mounts of the cab on the ride quality had been evaluated [7]. An optimal design for the cab's new rubber mounts of soil compactors was built via the finite element model, and the new rubber mount was then produced and tested for the vehicle's cab [6]. The dynamic parameters of the rubber mounts of the cab had been also optimized for improving the ride quality [8]. The research results concluded that the vehicle's ride quality was significantly improved. But, the study results also showed that the large-amplitude shock of the cab existed at low-frequency region in the direction of forwarding motion. This is one of the reasons causes tiredness of the driver

Based on the model of the vibratory roller dynamics in Fig. 1, the different dynamic equations of the vehicle are listed as follows:

$$m_s \ddot{z}_s = c_s(\dot{z}_c + \dot{\phi}_c l_1 - \dot{z}_s) + k_s(z_c + \phi_c l_1 - z_s), \quad (1)$$

$$m_c \ddot{z}_c = c_{c1}(\dot{z}_b + \dot{\phi}_c l_2 - \dot{\phi}_b l_6 - \dot{z}_c) + k_{c1}(z_b + \phi_c l_2 - \phi_b l_6 - z_c), \quad (2)$$

$$m_1 \ddot{z}_1 = c_d(\dot{z}_d - \dot{z}_1) + k_d(z_d - z_1), \quad (3)$$

$$m_b \ddot{z}_b = c_t(\dot{q}_{t1} - \dot{\phi}_b l_5 - \dot{z}_b) + k_t(q_{t1} - \phi_b l_5 - z_b) = 0, \quad (4)$$

$$I_c \ddot{\phi}_c = l_3 [c_{c2}(\dot{z}_b - \dot{z}_c - \dot{\phi}_c l_3 - \dot{\phi}_b l_4) + k_{c2}(z_b - z_c - \phi_c l_3 - \phi_b l_4)] \\ + l_2 [c_{c1}(\dot{z}_c - \dot{z}_b - \dot{\phi}_c l_2 + \dot{\phi}_b l_6) + k_{c1}(z_c - z_b - \phi_c l_2 + \phi_b l_6)] \\ + l_1 [c_s(\dot{z}_s - \dot{z}_c + \dot{\phi}_c l_1) + k_s(z_s - z_c + \phi_c l_1)], \quad (5)$$

$$I_b \ddot{\phi}_b = l_5 [c_t(\dot{q}_{t1} - \dot{z}_b - \dot{\phi}_b l_5) + k_t(q_{t1} - z_b - \phi_b l_5)] \\ - l_4 [c_{c2}(\dot{z}_c - \dot{z}_b + \dot{\phi}_c l_3 + \dot{\phi}_b l_4) + k_{c2}(z_c - z_b + \phi_c l_3 + \phi_b l_4)] \\ - l_6 [c_{c1}(\dot{z}_c - \dot{z}_b - \dot{\phi}_c l_2 + \phi_b l_6) + k_{c1}(z_c - z_b - \phi_c l_2 + \phi_b l_6)] \\ - l_7 [c_d(\dot{z}_1 - \dot{z}_d) + k_d(z_1 - z_d)]. \quad (6)$$

3. Modeling of Cab isolation systems

To evaluate the effect of the lumped parameters of the different isolation mounts of the cab including the RM, HM, and HPM, as plotted in Fig. 1, their mathematical models are then given in Fig. 2.

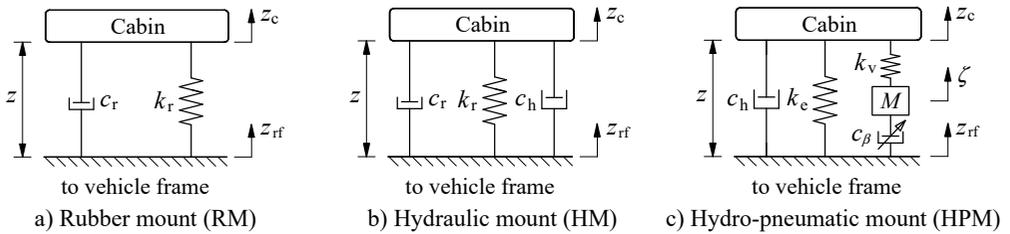


Fig. 2. The model of the different cab isolations

With the RM, as plotted in Fig. 1 and Fig. 2(a), it is made of rubber and metal and it can effectively isolate vibration by absorbing vibration energy. It is defined by a low damping coefficient c_r and high stiffness k_r . The corresponding vertical dynamic forces of the front and rear RMs are given as follows:

$$F_{ci} = c_{ri}(\dot{z}_{ci} - \dot{z}_{rfi}) + k_{ri}(z_{ci} - z_{rfi}), \quad \text{with RM.} \quad (7)$$

With the HM, as plotted in Fig. 1 and Fig. 2(b), it includes a main rubber material and a damper with its damping coefficient c_h used to isolate the vibration of the rear vehicle frame. Its mathematical equation is defined as follows [8, 9]:

$$F_{ci} = c_{ri}(\dot{z}_{ci} - \dot{z}_{rfi}) + k_{ri}(z_{ci} - z_{rfi}) + c_{hi}|\dot{z}_{ci} - \dot{z}_{rfi}|(\dot{z}_{ci} - \dot{z}_{rfi}), \quad \text{with HM.} \quad (8)$$

With the HPM, as shown in both Fig. 1 and Fig. 2(c), it includes an airbag used together with a damper to isolate the vibrations. In the mathematical model of Fig. 2(c), herein, k_v and k_e are the coefficients of the HPM's linear stiffness, c_β is the main damping parameter of the pneumatic mount, and c_h is the variable damping coefficient.

The corresponding vertical dynamic forces of the front and rear HPM are given as follows [5]:

$$F_{ci} = k_{ei}(\dot{z}_{ci} - \dot{z}_{rfi}) + c_{\beta i}|\dot{\zeta}_i|^{\beta i} \text{sign}(\dot{\zeta}_i) + M_i \ddot{\zeta}_i + c_{hi}|\dot{z}_{ci} - \dot{z}_{rfi}|(\dot{z}_{ci} - \dot{z}_{rfi}), \quad \text{with HM,} \quad (9)$$

$$\begin{cases} z_{ci} = z_{ci} + (-1)^{i+1} \phi_c l_{i+1}, \\ \dot{z}_{ci} = \dot{z}_{ci} + (-1)^{i+1} \dot{\phi}_c l_{i+1}. \end{cases} \quad (10)$$

$$\begin{cases} z_{rf1} = z_b + (l_1 + l_2 + l_3) \phi_b, \\ z_{rf2} = z_b - l_5 \phi_b, \end{cases} \quad \begin{cases} \dot{z}_{rf1} = \dot{z}_b + (l_1 + l_2 + l_3) \dot{\phi}_b, \\ \dot{z}_{rf2} = \dot{z}_b - l_5 \dot{\phi}_b, \end{cases} \quad (11)$$

where, z_{ci} and z_{rfi} in Eqs. (7-9) are the vertical displacements of suspension of cab and front and rear frames, $i = 1, 2$.

4. Vibration sources of the terrain and drum

4.1. The interaction model between the elastic/plastic soil and drum

Based on the result of Adam and Kop [2, 3], the interaction model between the elastic/plastic soil and drum has been built in Fig. 3, and the properties of the elastic and plastic of the soil ground have been expressed by the factors ε and γ as follows:

$$\varepsilon = \frac{k_{sp}}{k_{sp} + k_{se}}, \quad \gamma = \frac{c_{se}}{k_{sp}} \quad (12)$$

where, the parameters of ε , k_{se} , k_{sp} , and c_{se} are the compression ratio, elastic stiffness, compression stiffness, and compression damper.

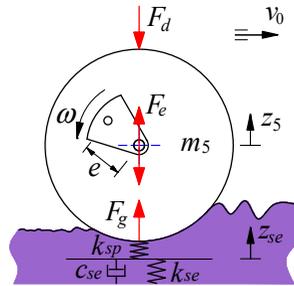


Fig. 3. The drum and elastic-plastic interaction

Based on the research results of Nguyen et al. [8-9], the interaction between the drum and deformable soil ground has been defined by three phases including loading phase, unloading phase, and drum-hope phase. The dynamic equations of three phases based on Refs. [7, 8] has been rewritten as follows:

$$\begin{cases} \varepsilon \gamma m_5 \ddot{z}_5 + m_5 \ddot{z}_5 = \varepsilon \gamma \dot{F}_d + F_d - \varepsilon c_{se} \dot{z}_5 + (\varepsilon - 1) k_{sp} z_5 \\ \quad + \varepsilon \gamma m_e e \omega^3 \cos \omega t + m_e e \omega^2 \sin \omega t, \end{cases} \quad (13)$$

$$\begin{cases} F_{dj} = k_{dj} [z_4 - z_5 + (-1)^j b_{j+3} (\theta_4 - \theta_5)] + c_{dj} [\dot{z}_4 - \dot{z}_5 + (-1)^j b_{j+3} (\dot{\theta}_4 - \dot{\theta}_5)], \\ m_5 \ddot{z}_5 = F_{dj} - c_{se} \dot{z}_5 + m_e e \omega^2 \sin \omega t, \end{cases} \quad (14)$$

$$m_5 \ddot{z}_5 = F_{dj} + mg + m_e e \omega^2 \sin \omega t, \quad j = 1, 2. \quad (15)$$

Eqs. (13-15) have been then used to calculate the motion of the drum z_5 and the excitation forces F_d .

4.2. The wheels-road surface roughness

Based on the ISO proposal [17], the terrain surface roughness $q(t)$ has given by $S(\Omega) = S(\Omega_0)(\Omega/\Omega_0)^{-w_0}$. Where $w_0 = 3$ with $\Omega \leq \Omega_0$, $w_0 = 2.25$ with $\Omega > \Omega_0$, $S(\Omega_0)$ is the

random terrain determined via the reference frequency of $\Omega_0 = 1/2\pi$ (cycle.m⁻¹).

Additionally, when the vehicle moving with a speed v_0 on the rough road, its road surface is then calculated via the series:

$$q(t) = \sum_{i=1}^N s_i \sin(i\Delta\omega t + \varphi_i), \quad (16)$$

where N is the number of intervals, $s_i = \sqrt{2S(i\Delta n)\Delta n}$ is the amplitude excitation harmonic, S is the target spectral density, $\Delta n = 2\pi/L$.

Based on the results of Mitschke [3], the excitation of the off-road terrain can be yielded by selecting a value in the spectral density ranges.

5. Simulations and discussions

At present, the evaluation of vehicle vibration is mainly divided into two categories including subjective and objective evaluation. Due to the complexity of people's subjective feelings, psychological and physiological characteristics need to be taken into account, and specialized personnel are needed to carry out the evaluation, so the subjective evaluation is subject to certain limitations. The objective evaluation method mainly considers the vibration isolation performance of the vehicle. The physical quantity of mechanical vibration (frequency, amplitude, acceleration, etc.) is taken as the evaluation index. Therefore, this objective evaluation is a widely used method. Vibration acceleration is the basic parameter for the ride comfort evaluation. According to the weighted root-mean-square (RMS) method of vibration acceleration recommended by ISO-2631, the RMS acceleration is calculated according to the following formula:

$$a_{wz} = \sqrt{\frac{1}{T} \int_0^T a_z^2(t) dt}, \quad (17)$$

where, T is the sampling time and $a(t)$ is the acceleration in the simulation process.

When vibratory rollers is moving or compressing on off-road grounds, the parameters of the stiffness and damping of the cab isolations, wheels, drum's isolations not only affect the stability, durability and safety, but also impact the vehicle's ride quality. Thus, the model of the vibratory roller is simulated to analyze the acceleration responses of the vertical driver's seat and the cab pitch angle with three cab isolations of the RM, HM, and HPM under different operation conditions of the vibratory roller.

5.1. Influence of the parameters of the cab isolations

To evaluate the performance of the cab isolations of the vibratory roller, based on the lumped parameters of the vibratory roller and cab isolation mounts in Tables 1 and 2, a single-drum vibratory roller working at the excitation frequency of the drum 28 Hz and 5 km/h on a hard soil ground is simulated. The simulation results of the acceleration responses of the vertical driver's seat and pitching cab angle are plotted in Fig. 4.

The results show that the acceleration responses of the vertical driver and pitching cab angle with the HPM is the smallest while that of the RM is the biggest. Therefore, the vehicle's ride comfort is strongly affected by the cab isolation system. To analyze the influence of the dynamic parameters of the isolations of the on the ride quality, the influence of the stiffness and damping parameters of the RM, HM, and HPM on the vibration of the vertical driver's seat and the cab shaking will being researched.

Table 1. The parameters of the vibratory rollers

Parameter	Value	Parameter	Value	Parameter	Value	Parameter	Value
m_s / kg	85	I_{cy} / kgm ²	523	l_4 / m	0.136	k_d / N m ⁻¹	3.9×10^6
m_c / kg	891	I_{by} / kgm ²	1.2×10^4	l_5 / m	0.76	k_t / N m ⁻¹	0.5×10^6
m_b / kg	2822	l_1 / m	0.383	l_6 / m	0.9	c_s / Ns m ⁻¹	1.2×10^2
m_1 / kg	4464	l_2 / m	0.1	l_7 / m	0.6	c_d / Ns m ⁻¹	2.9×10^3
m_d / kg	4378	l_3 / m	0.524	k_s / N m ⁻¹	1.2×10^4	c_t / Ns m ⁻¹	4.0×10^3

Table 2. The parameters of the cab isolation mounts

Parameter	Value	Parameter	Value	Parameter	Value
k_{r1} / Nm ⁻¹	9.1×10^5	k_{p1} / Nm ⁻¹	15.3×10^5	$c_{\beta 1}$ / Ns ² m ⁻²	12.4×10^3
k_{r2} / Nm ⁻¹	1.2×10^5	k_{p2} / Nm ⁻¹	2.01×10^5	$c_{\beta 2}$ / Ns ² m ⁻²	10.7×10^3
M_1 / kg	98	c_{r1} / Nsm ⁻¹	218	c_{h1} / Ns ² m ⁻²	20×10^3
k_{e1} / Nm ⁻¹	9.1×10^5	c_{r2} / Nsm ⁻¹	29	c_{h2} / Ns ² m ⁻²	4.5×10^3
k_{e2} / Nm ⁻¹	1.2×10^5	M_2 / kg	33	ε	0.87

Table 3. The parameters of the elastoplastic ground with its hard soil

Parameter	Value	Parameter	Value
k_{sp} / N m ⁻¹	283×10^6	ω_0	2.14
c_{se} / Ns m ⁻¹	37.1×10^3	$S(m_0)$ / m ³ cyc ⁻¹	3782.5×10^{-6}

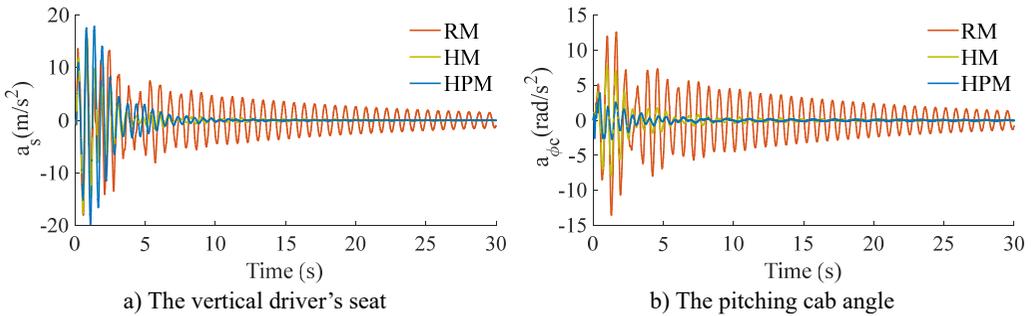


Fig. 4. The acceleration responses under a hard soil ground

5.1.1. Influence of the stiffness parameters

Under the same simulation condition of $v = 5$ km/h of the vehicle and $f = 28$ Hz of the drum on the hard soil ground, the different stiffness of the cab isolations $K_c = [0.2, 0.4, \dots, 2.0] \times K_{c0}$ with the RM, HM, and HPM is selected to simulate the result. The effect of the different stiffness of the suspension system of the vehicle on the RMS acceleration responses of the vertical driver's seat (a_{wzs}) and pitching cab angle ($a_{w\phi c}$) is shown in Fig. 5.

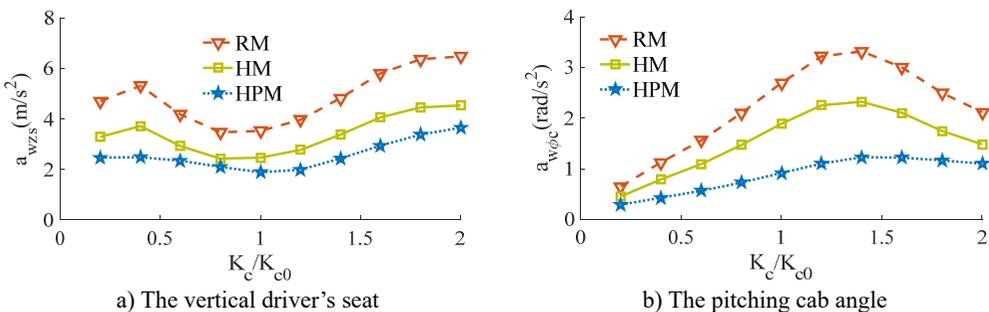


Fig. 5. The RMS acceleration responses under the different stiffness coefficients

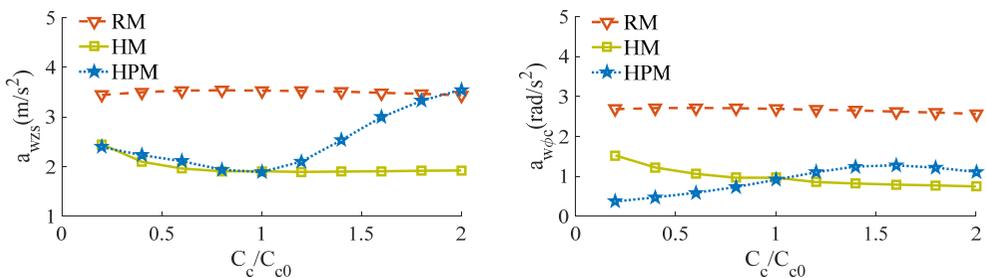
The RMS acceleration response of the vertical driver's seat (a_{wz}) in Fig. 5(a) shows that when the stiffness of the cab isolations is increased from $0.2 \times K_{c0}$ to $0.8 \times K_{c0}$, the a_{wz} is slightly reduced. When the stiffness value is increased from $1.2 \times K_{c0}$ to $2.0 \times K_{c0}$, the a_{wz} is strongly increased. With the stiffness values from $0.8 \times K_{c0}$ to $1.2 \times K_{c0}$, the a_{wz} with all three RM, HM, and HPM is the smallest. This means that the vertical vibration of the driver's seat is greatly improved. Besides, the RMS acceleration response of the pitching cab angle ($a_{w\phi c}$) in Fig. 5(b) shows that when the stiffness of the cab isolations is increased from $0.2 \times K_{c0}$ to $1.4 \times K_{c0}$, the $a_{w\phi c}$ is strongly increased. When the stiffness value is increased from $1.4 \times K_{c0}$ to $2.0 \times K_{c0}$, the $a_{w\phi c}$ is significantly reduced. With the stiffness value of $K_c = 1.4 \times K_{c0}$, the $a_{w\phi c}$ is the biggest. Thus, the cab shaking is also the biggest. The comparison results between the RM, HM, and HPM in Fig. 5 show that both the a_{wz} and $a_{w\phi c}$ with the HPM is the smallest under the different stiffness coefficients. Therefore, the vehicle's ride comfort is greatly improved by using the HPM. Additionally, a stiffness range of $K_c = [0.8 \text{ to } 1.2] \times K_{c0}$ should be chosen to further improve the vehicle's ride comfort and control the cab shaking.

5.1.2. Influence of the damping parameters

The different damping's of $C_{c0} = [0.2, 0.4, \dots, 2] \times C_{c0}$ with three various isolations of the RM, HM, and HPM are simulated under the same simulation condition of Section 5.1.1. The simulation results are shown in Fig. 6.

The result shows that both the a_{wz} and $a_{w\phi c}$ with the RM is insignificantly changed with the different damping coefficients of the RM. This is due to the c_r value of the RM is very small. With the change of the c_h values, both the a_{wz} and $a_{w\phi c}$ are significantly reduced when increasing the c_h values, thus, the driver's ride comfort and cab shaking is also improved by the increasing damping coefficient of the HM.

With the HPM, when the damping value is increased from $0.5 \times C_{c0}$ to $1.0 \times C_{c0}$, both the a_{wz} and $a_{w\phi c}$ are slightly reduced and smaller than that of the HM. Conversely, with the damping value of the HPM increased from $1.0 \times C_{c0}$ to $2.0 \times C_{c0}$, both the a_{wz} and $a_{w\phi c}$ are strongly increased and higher than that of the HM, thus, the vehicle's ride comfort is greatly reduced. Based on the analysis results, the damping range of $C_c = [0.8 \text{ to } 1.0] \times C_{c0}$ should be chosen to further improve the vehicle's ride comfort and control the cab shaking with the HPM.

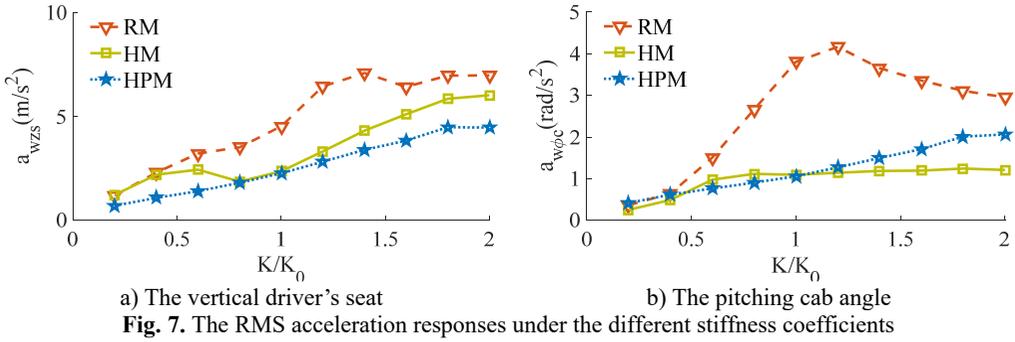


a) The vertical driver's seat
 b) The pitching cab angle
Fig. 6. The RMS acceleration responses under the different damping coefficients

5.2. Influence of the parameters of the wheel and drum's isolations

5.2.1. Influence of the stiffness parameters

Under the same simulation condition of $v = 5$ km/h of the vehicle and $f = 28$ Hz of the drum on the hard soil ground, the stiffness effect of the tires and drum isolations $K_{t,d} = [0.2, 0.4, \dots, 2.0] \times K_{t0,d0}$ on the a_{wz} and $a_{w\phi c}$ is also obtained, as shown in Fig. 7.

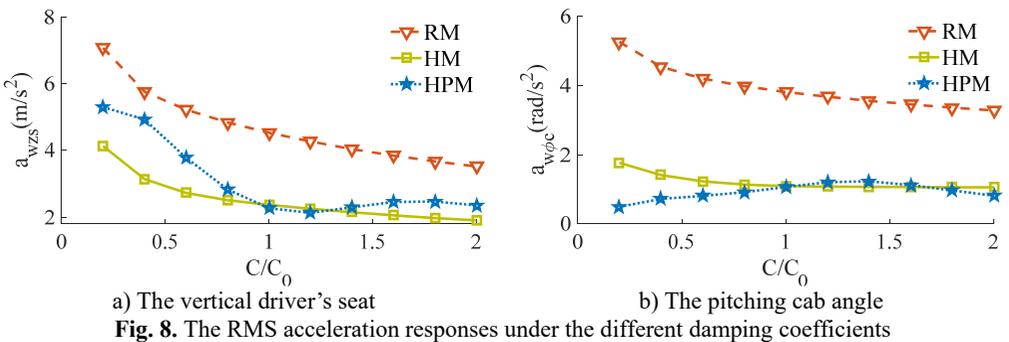


The simulation results indicate that both the a_{wzs} and a_{wpc} with all the RM, HM, and HPM are quickly increased with the increase of the stiffness coefficient of both the tires and drum isolations from $0.2 \times K_{t0,d0}$ to $2.0 \times K_{t0,d0}$. Thus, the vertical driver's ride comfort and cab shaking is greatly reduced. To improve the vehicle's ride comfort, the stiffness value of the tires and drum isolations should be chosen by $K_{t,d} = [0.6 \text{ to } 1.0] \times K_{t0,d0}$. Additionally, the performance of the HPM on the improvement of the vehicle's ride comfort is insignificantly affected under the different stiffness values of the tires and drum isolations.

5.2.2. Influence of the damping parameters

Similarly, the effect of the different damping's of the tires and drum isolations $C_{t,d} = [0.2, 0.4, \dots, 2.0] \times C_{t0,d0}$ on the a_{wzs} and a_{wpc} is simulated under the same condition of $v = 5 \text{ km/h}$ of the vehicle and $f = 28 \text{ Hz}$ of the drum on the hard soil ground. The simulation results are shown in Fig. 8.

The simulation results show that both the a_{wzs} and a_{wpc} with all the RM, HM, and HPM are significantly affected by the dampings of the tires and drum isolations. When the damping coefficients of the tires and drum isolations are increased from $0.2 \times C_{t0,d0}$ to $2.0 \times C_{t0,d0}$, both the a_{wzs} and a_{wpc} with both the RM and HM are reduced. However, the comparison result between the HM and HPM shows that with $C_{t,d} = [0.2 \text{ to } 1.0] \times C_{t0,d0}$ and $C_{t,d} = [1.4 \text{ to } 2.0] \times C_{t0,d0}$, the a_{wzs} of the HPM is higher than the HM, thus, the vehicle's ride comfort is reduced by using the HPM. To improve the vehicle's ride comfort and cab shaking, the damping coefficients of the tires and drum isolations should be also chosen by $C_{t,d} = [1.0 \text{ to } 1.2] \times C_{t0,d0}$.



6. Conclusions

Based on the simulation results of the effect of the vehicle and cab isolations' parameters on the improvement of the ride comfort and cab shaking with three cab isolations of the RM, HM,

and HPM in this paper, a conclusion can be drawn:

- 1) The different dynamic parameters of the vehicle and cab isolations have significant effect on the ride comfort of the vibratory roller.
- 2) Under the different simulation conditions of the dynamic parameters, the vehicle's ride comfort and cab shaking with the HPM is better improved compared to both the RM and HM.
- 3) To optimize the vehicle's ride comfort, the stiffness and damping parameters of the cab isolations, tires, and drum isolations should be designed in a range of $K_c = [0.8 \text{ to } 1.2] \times K_{c0}$, $C_c = [0.8 \text{ to } 1.0] \times C_{c0}$, $K_{t,d} = [0.6 \text{ to } 1.0] \times K_{t0,d0}$, and $C_{t,d} = [1.0 \text{ to } 1.2] \times C_{t0,d0}$.
- 4) To further improve the vehicle's ride comfort and control the cab shaking, the HPM with the damping coefficient of the hydraulic mount will be studied and controlled in Part-2.

Acknowledgments

This research was supported by Open Fund Project of Hubei Key Laboratory of Intelligent Transportation Technology and Device, Hubei Polytechnic University, China (No. 2020XY105) and Talent Introduction Fund Project of Hubei Polytechnic University (No. 19XJK17R), and Research Project of Hubei Polytechnic University, China (No. 18XJZ05Q).

References

- [1] **Bekker M.** Introduction to Terrain-Vehicle Systems. University of Michigan Press, Ann Arbor, USA, 1969.
- [2] **Wong J.** Theory of Ground Vehicles. John Wiley and Sons, New York, NY, USA, 2001.
- [3] **Mitschke M.** Dynamik Der Kraftfahrzeuge. Springer-Verlag, Berlin, Germany, 1972.
- [4] **Nguyen V., Zhang J., et al.** Effect of the off-road terrains on the ride comfort of construction vehicles. Journal of Southeast University, Vol. 35, Issue 2, 2019, p. 191-197.
- [5] **Nguyen V., Zhang J., et al.** Vibration analysis and modeling of an off-road vibratory roller equipped with three different cab's isolation mounts. Shock and Vibration, Vol. 2018, 2018, p. 8527574.
- [6] **Li J. Q., Zhang Z. F., Xu H. G., Feng Z. X.** Dynamic characteristics of the vibratory roller test-bed vibration isolation system: Simulation and experiment. Journal of Terramechanics, Vol. 56, 2014, p. 139-156.
- [7] **Nguyen V., Zhang J., et al.** Ride quality evaluation of the soil compactor cab supplemented the auxiliary hydraulic mounts via simulation and experiment. Journal of Central South University, Vol. 35, 2019, p. 273-280.
- [8] **Nguyen V., Nguyen K.** Enhancing the ride comfort of the off-road vibratory roller cab by adding damper hydraulic mount. Vibroengineering Procedia, Vol. 21, 2018, p. 89-95.
- [9] **Jiao S. J., Wang Y., Zhang L., Hua H.** Shock wave characteristics of a hydraulic damper for shock test machine. Mechanical Systems and Signal Processing, Vol. 24, 2010, p. 1570-1578.
- [10] **Lee P., Vogt J., Han S.** Application of hydraulic body mounts to reduce the freeway hop shake of pickup truck. SAE Technical Paper Series, 2009-01-2126, 2009.
- [11] **Nguyen V., Zhang J., et al.** Low-frequency performance of semi-active cab's hydraulic mounts of an off-road vibratory roller. Shock and Vibration, Vol. 2019, 2019, p. 8725382.
- [12] **Nguyen V., Jian R., et al.** Performance analysis of semi-active hydraulic system of the off-road vibratory roller cab using optimal fuzzy-PID control. Journal of Central South University, Vol. 35, 2019, p. 399-407.
- [13] **Seo J. U., Yun Y. W., Park M. K.** Magneto-rheological accumulator for temperature compensation in hydro-pneumatic suspension systems. Journal of Mechanical Science and Technology, Vol. 25, 2011, p. 1621-1625.
- [14] **Danish A., Samuel F.** Artificial intelligence models for predicting the performance of hydropneumatic suspension struts in large capacity dump trucks. International Journal of Industrial Ergonomics, Vol. 67, 2018, p. 283-295.
- [15] **Nguyen V., Zhang J., et al.** Low-frequency ride comfort of vibratory rollers equipped with cab hydro-pneumatic mounts. Journal of Southeast University, Vol. 36, Issue 3, 2020, p. 278-284.
- [16] **Jiao R., Nguyen V., Le V.** Ride comfort performance of hydro pneumatic isolation for soil compactors cab in low frequency region. Journal of Vibroengineering, Vol. 22, 2020, p. 1174-1186.
- [17] **Griffin M.** Handbook of Human Vibration. Academic Press, London, UK, 1990.

- [18] **Nguyen V., Jiao R., Zhang J.** Control performance of damping and air spring of heavy truck air suspension system with optimal fuzzy control. *Journal of Vehicle Dynamics, Stability, and NVH*, Vol. 4, 2020, p. 179-194.
- [19] **Yuan H., Nguyen V., Zhou H.** Research on semi-active air suspensions of heavy trucks based on a combination of machine learning and optimal fuzzy control. *Journal of Vehicle Dynamics, Stability, and NVH*, 2021, (in Press).



Yan Kang is the student at School of Mechanical and Electrical Engineering, Hubei Polytechnic University, Huangshi City, China. Her current research interests include Vehicle dynamics and control vibration.



Vanliem Nguyen received Ph.D. degree in School of Mechanical Engineering, Southeast University, Nanjing, China, in 2018. His current research interests include vehicle dynamics, vibration and optimization control, lubrication and tribology. ORCID iD: <https://orcid.org/0000-0001-8772-1086>.



Xiaoyan Guo is the teacher at School of Mechanical and Electrical Engineering, Hubei Polytechnic University, Huangshi City, China. Her current research interests include the nonlinear mathematical models and numerical optimizations.



Yuehan Li is the student at School of Mechanical and Electrical Engineering, Hubei Polytechnic University, Huangshi City, China. His current research interests include Vehicle dynamics and control vibration.