An assembled hot wire anemometer design

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Received 15 September 2023; accepted 28 December 2023; published online 3 January 2024
DOI https://doi.org/10.21595/me.2023.23637

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Abstract. The hot wire anemometer is a widely utilized device in laboratory settings for measuring air speed. This paper investigates the relationship between air speed and hot wire temperature across various air speed ranges, employing the theory of thermal equilibrium. We designed a measurement circuit and hot wire shape based on the hot wire anemometer principle, and validated the linear relationship between current and temperature at different air speeds within an adjustable air speed field. The measured current serves as a representative of air speed. Experimental validation of the designed hot wire anemometer demonstrates accurate measurement results that align with theoretical values across different air speed ranges. Finally, we determined the sensitivity of the anemometer in various measurement ranges, considering the instrument's uncertainty and measurement formula.

Keywords: hot wire, anemometer, uncertainty, sensitivity.

1. Introduction

The precise measurement of air speed plays a crucial role in both laboratory and engineering applications [1]. Accurate assessments are fundamental to understanding fluid dynamics, optimizing aerodynamic performance, and enhancing various industrial processes. A myriad of instruments are employed for air speed measurement, including mechanical anemometers, laser Doppler anemometers, ultrasonic anemometers, particle image velocimetry, and hot-wire anemometers [2]-[7]. Among these, hot-wire anemometers stand out due to their notable advantages: a broad measurement range, rapid measurement speed, and high sensitivity [8]. The operating principle of a hot-wire anemometer is rooted in the generation of heat when an electric current passes through a thin wire. As the wind flows over the hot wire, forced convection from the wire dissipates heat, resulting in a decrease in wire temperature and resistance. The air speed is then determined by establishing the relationship between pertinent physical quantities. This type of anemometer has gained widespread acceptance in both research and industrial applications owing to its accuracy, reliability, and operational convenience [9]-[13]. While computer simulations have been instrumental in studying the behavior of hot-wire anemometers under various conditions [14]-[17], recent advancements in the field call for attention. Scholars have delved into visualizing and analyzing scenarios involving different forms of hot wires in diverse environmental conditions [18]-[21]. Notably, Pankaj Charan Jena's work emphasizes the pivotal role of heat exchangers in various industries and underscores the need for advanced designs to meet current industrial demands [22]. The study proposes a modeling and design approach utilizing the finite element method, specifically computational fluid dynamics. ANSYS 15.0 is employed to analyze the heat transfer rate of shell and tube-type heat exchangers, incorporating vertical baffles in the design and simulation. The research contributes valuable insights into the selection of input parameters, modeling techniques, and simulation methodologies.

In the present study, we delve into the design of a multi-range anemometer, incorporating self-designed hot wires and measurement circuits. Our focus lies in optimizing design parameters to ensure measurement sensitivity while addressing the limitations observed in existing hot-wire anemometer models. By developing an innovative approach, we aim to contribute to the refinement of air speed measurement techniques, fostering advancements in fluid dynamics.
research and enhancing the applicability of such instruments in various scientific and industrial domains.

2. Theoretical basis

Generally, heat exchange between a heated wire and its surroundings manifests in four modes: natural convection, forced convection, heat conduction, and thermal radiation. Taking into account a scenario where the wire is subjected to external heating (e.g., electrical current) and subsequently dissipates heat through all the aforementioned mechanisms to its surroundings, the power balance equation can be articulated upon achieving thermal equilibrium in the system:

\[ P_{\text{Input}} = P_{\text{Forced convection}} + P_{\text{Natural convection}} + P_{\text{Heat conduction}} + P_{\text{Heat radiation}}, \]

\[ i^2 R_e = h A_w (T - T_0) + P_{\text{Natural convection}} + P_{\text{Heat conduction}} + A_w \sigma \varepsilon (T^4 - T_0^4). \]

Because the length of the hot wire is much larger than its cross section, the heat transfer caused by conduction is negligible. For small temperature changes there is \( T^4 - T_0^4 = T_0^3 (T - T_0) \). \( P_{\text{Natural Convection}} \) can be considered constant. Eq. (2) is rewritten as:

\[ i^2 R_e = h' A_w (T - T_0), \]

where: \( A_w \) is the surface area of the electric heating wire; \( T_0 \) is the ambient temperature, \( T \) is the temperature of the heating wire at a specific power; \( \sigma \) is the Stefan-Boltzmann constant, \( \varepsilon \) is the emissivity; \( h \) is the forced convection heat conversion coefficient, \( h' \) is the equivalent heat conversion coefficient. From King’s law in thermodynamics, the following equation is known when the air speed is high:

\[ \frac{dH}{dt} = i^2 R_e - (K + C \sqrt{V})(T - T_0). \]

When air speed is low:

\[ \frac{dH}{dt} = i^2 R_e - \frac{M}{N - \ln V}(T - T_0), \]

where: \( V \) represents air speed; \( H \) represents heat; and \( dH/dt \) represents the rate of heat dissipation. \( i \) represents the current in the resistance wire. \( R_e \) represents the instantaneous resistance at a given time. \( T_0 \) is the ambient temperature at that time. \( K, C, M, \) and \( N \) are constant parameters.

When the temperature of the hot wire reaches thermal equilibrium: \( dH/dt = 0 \), and the air speed in the high air speed case can be obtained as:

\[ i^2 R_e = (K + C \sqrt{V})(T - T_0). \]

Because the resistance satisfies a linear relationship with temperature near room temperature:

\[ R_e = R_0 [1 + \alpha (T - T_0)]. \]

Substituting Eq. (7) into Eq. (6), we get:

\[ T_e (V) - T_0 = \frac{i^2 R_0}{K + C \sqrt{V} - \alpha i^2 R_0}. \]
where \( R_0 \) is the resistance value at temperature \( T_0 \) and \( \alpha \) is the resistance temperature coefficient. From this we can get:

\[
\Delta T = T_e(0) - T_e(V) = \frac{i^2 R_0}{K - \alpha i^2 R_0} - \frac{i^2 R_0}{K + C \sqrt{V} - \alpha i^2 R_0}.
\]  

(9)

After sorting, we get:

\[
\frac{1}{\sqrt{V}} = \frac{Ci^2 R_0}{(K - \alpha i^2 R_0)^2} \frac{1}{\Delta T} - \frac{1}{i^2 R_0}.
\]  

(10)

In the same way, the relationship between air speed and temperature variation for smaller air speeds can be obtained as follows:

\[
\frac{1}{\ln(V)} = \frac{MN \alpha i^2 R_0}{N(N \alpha i^2 R_0 - M)^2} \frac{1}{T_e(V) - T_e(V = 1)} + \frac{\alpha i^2 R_0}{N \alpha i^2 R_0 - M}.
\]  

(11)

The constant parameters associated with the instrument are simplified to obtain the relationship between \( V \) and \( T \) satisfied at high and low air speeds.

High air speed:

\[
\frac{1}{\sqrt{V}} = A_{\text{high}} * \frac{1}{\Delta T} + B_{\text{high}}.
\]  

(12)

Low air speed:

\[
\frac{1}{\ln(V)} = A_{\text{low}} * \frac{1}{T_e(V) - T_e(V = 1)} + B_{\text{low}}.
\]  

(13)

Eqs. (12-13) give the relationship between air speed and temperature at different air speeds.

3. Design scheme

3.1. Design route

The apparatus comprises four integral modules: an air speed field environment module, a standard air speed measurement module, a temperature measurement module, and a circuit measurement module. A variable wind field is generated through a blower, while a standard anemometer is employed to gauge the air speed precisely at the hot wire's location. Infrared thermal imaging is utilized for capturing the temperature of the hot wire. The circuit is intricately engineered to convert variations in resistance, stemming from temperature fluctuations in the hot wire, into corresponding alterations in circuit current. This facilitates the establishment of a relationship between current and air speed. The design systematically addresses instrumental system errors and the microamp file sensitivity of the digital multimeter, ensuring the selection of optimal parameters for the associated instruments. Fig. 1 illustrates the nuanced design concepts in detail.

The hot wire is intricately integrated into the circuit, arranged in parallel with a resistor box. A digital multimeter, along with an adjustable voltage source, is serially connected to the resistor box branch, and the entire circuit is powered by a current source. Measurement of the current within the resistor box is facilitated by the microampere scale of the digital multimeter, thereby enabling the determination of the hot wire’s resistance variations. The circuit configuration is visually depicted in Fig. 2. Eq. (14) succinctly captures the system dynamics derived from the
interplay of voltages across the two branches and the circulating current within the circuit:

\[ I_r r = I'(R + R_A) + U, \]
\[ U = I_r + I'. \] (14)

![Fig. 1. Experimental design idea diagram](image1)

![Fig. 2. Circuit design diagram](image2)

The digital multimeter’s microamp setting reads:

\[ I' = \frac{I r - U}{R + R_A + r'} \] (15)

where \( I \) is the current of the current source; \( I' \) is the current of the digital multimeter; \( I_r \) is the current flowing through the hot wire; \( r \) is the resistance of the hot wire; \( R \) is the resistance value of the resistance box; \( R_A \) is the internal resistance of the digital multimeter; \( U \) is the voltage of the voltage source.

Adjust the voltage source so that when there is no wind the digital multimeter microamp gear indicates 0. Then there is \( r = \frac{U}{I} \). Assume that when there is a wind field, the electric heating wire resistance changes to \( \Delta r \), the digital multimeter microamp gear indicates the following:

\[ \Delta I = \frac{I \Delta r}{R + R_A + r'} \] (16)

Therefore, the variation of the resistance of the hot wire can be obtained as:

\[ \Delta r = \frac{(R_A + R + \frac{U}{T}) \Delta I}{I - \Delta I}. \] (17)

Upon scrutiny of Eq. (16), it becomes evident that the resistance value, denoted as \( R \) in this circuit, significantly influences the measurement sensitivity of the system. A diminutive \( R \)
amplifies the sensitivity, making the circuit more responsive to unit changes in current-induced 
resistance alterations, albeit at the cost of heightened measurement uncertainty. Conversely, a 
larger $R$ diminishes circuit uncertainty, albeit at the expense of reduced sensitivity. Consequently, 
a meticulous analysis of uncertainty is imperative to ascertain the optimal $R$ value. The relative 
uncertainty, articulated in Eq. (17), is derived as follows:

$$
\frac{U_{\Delta r}}{\Delta r} = \sqrt{\sum_{i=U, I, \Delta I, R_1, R_2} \left( \frac{\partial \ln \Delta r}{\partial I} U_i \right)^2}.
$$  \hspace{1cm} (18)

The uncertainties of the relevant instruments are known from the sensitivity of the instruments 
as follows: $U_{R+R_A} = 0.1$ $\Omega$, $U_I = 0.001$ A, $U_U = 0.01$ V, $U_{\Delta I} = 0.1$ $\mu$A.

After bringing them into Eq. (18), we get:

$$
U_{\Delta r} = \sqrt{2 \left( \frac{1}{1000} \right)^2 + \left( \frac{1}{10R} \right)^2}.
$$  \hspace{1cm} (19)

The sensitivity of hot wire resistance measurement can be obtained from Eq. (17):

$$
S_{\Delta r} = \frac{d\Delta r}{d\Delta I} = \frac{I(R_A + R) + U}{(I - \Delta I)^2}.
$$  \hspace{1cm} (20)

Considering that the resolution of the multimeter is 0.1 $\mu$A; it is necessary to control $\Delta I$ in the 
range of 0-500 $\mu$A. Therefore, the measurement sensitivity is $S_{\Delta r} \approx R \times 1 \times 10^{-7}$. When the 
sensitivity and uncertainty are equal, $R \approx 10^4$ $\Omega$; the measurement sensitivity of the resistance is
obtained as $10^{-3}$ $\Omega$. When gradually increasing the air speed, there is an extremely obvious change 
in the current expression. Therefore, it shows that the circuit and the experimental setup can be 
used to measure the air speed.

### 3.2. Apparatus and materials

The experimental apparatus, illustrated in Fig. 3, encompasses the utilization of specific 
instruments and materials. A blower with adjustable air speed (LEYBOLD DIDACTIC GMBH, 37304) serves as the air speed field environment module. The standard air speed measurement 
module incorporates a SMART SENSOR anemometer (ST866A) strategically positioned near the 
hot wire, as depicted in Fig. 4.

![Fig. 3. The assembled hot wire anemometer apparatus](image.png)

For temperature measurement, an infrared thermal imaging camera (FOTRIC, 224s) is
employed to capture comprehensive temperature changes in the hot wire. The circuit measurement module is comprised of essential components: two power supplies (UNI-T,3315TFL-II) functioning as a constant current source to ensure circuit stability and a constant voltage source for adjusting reverse voltage, a VICTOR digital multimeter (VC9805A) for measuring weak current, and a resistor box with adjustable resistance based on design accuracy. Furthermore, the resistor box allows precise adjustment of resistance values in accordance with the experimental design. The hot wire, formed by winding a 0.200 mm diameter iron wire into a spiral shape with dimensions of 8.00 mm in diameter and 35.00 mm in length, is affixed to a bracket, as shown in Fig. 5. The experimental conditions maintain a temperature of 25.0 ℃ and humidity ranging between 58 % to 63 %.

4. Results and discussion

4.1. Relationship between current and temperature

The thermal characteristics of the hot wire were documented through infrared thermography, and the corresponding temperatures were systematically recorded. Fig. 6 illustrates the thermal profile of the hot wire captured by the infrared thermal imaging camera. Concurrently, the current flowing through the circuit was meticulously recorded using the current mode of the digital multimeter. Subsequently, a temperature-current graph was generated, depicted in Fig. 7, wherein different air speed conditions were considered.

The current was subjected to a linear fit against temperature to ascertain its slope

\[ \beta_{\text{exp}} = \frac{\Delta I}{\Delta T} = (1.86 \pm 0.02) \mu \text{A/K}. \]

Theoretical value \( \beta_{\text{the}} = \frac{\Delta I}{\Delta T} = \frac{10^{-6}(R_A + R_L)U}{(I - \Delta I)R_e(0)} = 1.84 \mu \text{A/K}, \) as per...
Eq. (7) and (17), were compared with experimental results, revealing a notable consistency between the two. The observed linear relationship between current and temperature, coupled with the convergence of theoretical and experimental outcomes within the margin of error, underscores the viability of employing current as a means to characterize temperature. This concurrence supports the exploration of the experimental relationship between air speed and temperature through current analysis.

4.2. Relationship between the air speed and hot wire temperature

The air speed in proximity to the hot wire was quantified using an anemometer, while the temperature of the hot wire was systematically documented employing a thermal imaging camera. Concurrently, the current coursing through the constant-value resistor box was precisely registered using a digital multimeter within the microampere range. The datasets of current and temperature, acquired under various air speed conditions, are graphically depicted in Fig. 8.

According to the Eqs. (12-13) the digital multimeter microamp gear indication and the thermal wire temperature taken by the infrared camera were fitted in two different intervals of low and high air speed, as shown in Fig. 9. The correlation coefficients and expressions can be obtained as follows.

High air speed: \( \frac{1}{\sqrt{V}} = \frac{550}{\Delta T} - 2.6; R^2 = 0.975. \)

Low air speed: \( \frac{1}{\ln(V)} = \frac{66.1}{T_e(V) - T_e(V=1)} - 0.18; R^2 = 0.991. \)

From the correlation coefficient \( R^2 \) it can be seen that the data fitting results are in general agreement with the theoretical formula. Therefore, the hot wire anemometer can be designed for different air speed intervals according to this formula.
4.3. Anemometer sensitivity analysis

From the previous analysis of the sensitivity of resistance measurement, it is clear that the minimum division of temperature is: 

\[ S_T = \frac{\Delta r_{\text{min}}}{\Delta T} \approx 5 \times 10^{-2} \text{ K.} \]

When the air speed is in the range of 0-1.00 m/s, the measurement sensitivity is 

\[ \Delta V_{\text{min}} = \left( \frac{dU}{dl} \right) * \beta * S_T \approx 0.001 \text{ m/s.} \]

When the air speed is greater than 1.00 m/s:

\[
\Delta V_{\text{min}} = \left( \frac{dU}{dl} \right)_{V>1 \text{m/s}} * \beta * S_T = \frac{2A_{\text{high}} * \frac{1}{\Delta T} * \beta * S_T}{(A_{\text{high}} * \frac{1}{\Delta T} + B_{\text{high}})^3}. \tag{21}
\]

The relationship between air speed measurement sensitivity and the air speed range is delineated by Eq. (21). Notably, a simple anemometer exhibits variable sensitivity across distinct air speed intervals, with sensitivity diminishing as air speed increases. Consequently, the worst sensitivity within each interval serves as the basis for establishing three discrete measurement sensitivities across the air speed spectrum. The ensuing outcomes are presented in Table 1.

<table>
<thead>
<tr>
<th>Table 1. Measurement sensitivity of different ranges of anemometer</th>
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<tr>
<td>Measurement sensitivity (m/s)</td>
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<tr>
<td>-------------------------------</td>
</tr>
<tr>
<td>0.001</td>
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<tr>
<td>0.01</td>
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5. Conclusions

Grounded in the foundational principles of thermal equilibrium, our research embarked on a comprehensive investigation into the intricate relationship between hot wire temperature and air speed. Our methodical approach encompassed the creation of a variable air speed field, the meticulous construction of a bespoke hot wire, the design of an innovative measurement circuit, and the seamless integration of these components into an advanced air speed meter. To probe the correlation between current and temperature, we leveraged both a standard anemometer and an infrared thermal imager, employing these tools to scrutinize the dynamic interplay between air speed and the resultant thermal effects on our custom hot wire. The acquired data was subjected to rigorous analysis, allowing us to not only establish but also validate the anticipated relationship between air speed and current across diverse ranges. Remarkably, the experimental results consistently mirrored the predictions derived from theoretical considerations, affirming the
robustness and reliability of our developed air speed meter. One noteworthy aspect of the investigation was the meticulous calculation of measurement sensitivity across various air speed ranges. This involved a nuanced consideration of the smallest scale of selected instruments and the inherent uncertainty associated with theoretical formulas. The air speed meter demonstrated exceptional measurement sensitivity, emerging as a dependable instrument capable of furnishing precise data across a spectrum of air speed conditions. Moreover, the study shed light on the linear relationship between temperature and current in the microampere meter, unveiling the potential utility of electric current as a means for accurate temperature measurements in similar experimental setups. This finding not only enhances the versatility of our air speed meter but also opens avenues for further exploration into leveraging electric current for nuanced temperature assessments.

In summation, our research yields compelling evidence regarding the effectiveness and reliability of the developed air speed meter. Beyond serving as a testament to the meticulousness of our methodology, the study contributes invaluable insights into air speed measurement methodologies, setting the stage for continued exploration into the multifaceted applications of electric current in the realm of precise temperature measurements. This innovative approach not only advances the field of fluid dynamics but also holds promise for diverse scientific and industrial applications where accurate air speed measurement is of paramount importance.

Acknowledgements

This project is funded Experimental Technology Research Project of Zhejiang University in 2022 (SYBJS20220205).

Data availability

The datasets generated during and/or analyzed during the current study are available from the corresponding author on reasonable request.

Author contributions

Xingxing Yao: funding acquisition, investigation, resources, validation, writing-review and editing, writing-review and editing. Fanhao Shen: conceptualization, data curation, formal analysis. Yuan Zheng: resources, writing-review and editing. Ting Xiao: investigation, writing-review and editing.

Conflict of interest

The authors declare that they have no conflict of interest.

References

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10 ISSN PRINT 2335-2124, ISSN ONLINE 2424-4635


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